

Package ‘DisImpact’

September 2, 2021

Title Calculates Disproportionate Impact When Binary Success Data are Disaggregated by Subgroups

Version 0.0.15

Description Implements methods for calculating disproportionate impact: the percentage point gap, proportionality index, and the 80% index. California Community Colleges Chancellor's Office (2017). Percentage Point Gap Method. <<https://www.cccco.edu/-/media/CCCCO-Website/About-Us/Divisions/Digital-Innovation-and-Infrastructure/Research/Files/PercentagePointGapMethod2017.ashx>>. California Community Colleges Chancellor's Office (2014). Guidelines for Measuring Disproportionate Impact in Equity Plans. <<https://www.cccco.edu/-/media/CCCCO-Website/Files/DII/guidelines-for-measuring-disproportionate-impact-in-equity-plans-tfa-ada.pdf>>.

Depends R (>= 3.4.0)

Imports dplyr (>= 0.8.5), rlang, tidyselect, purrr, tidyr

License GPL-3

URL <https://github.com/vinhdizzo/DisImpact>

BugReports <https://github.com/vinhdizzo/DisImpact/issues>

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di_80_index	<i>Calculate disproportionate impact per the 80% index</i>
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Description

Calculate disproportionate impact per the 80% index method.

Usage

```
di_80_index(
  success,
  group,
  cohort,
  weight,
  data,
  di_80_index_cutoff = 0.8,
  reference_group = "hpg",
  check_valid_reference = TRUE
)
```

Arguments

success	A vector of success indicators (1/0 or TRUE/FALSE) or an unquoted reference (name) to a column in data if it is specified. It could also be a vector of counts, in which case weight should also be specified (group size).
group	A vector of group names of the same length as success or an unquoted reference (name) to a column in data if it is specified.
cohort	(Optional) A vector of cohort names of the same length as success or an unquoted reference (name) to a column in data if it is specified. disproportionate impact is calculated for every group within each cohort. When cohort is not specified, then the analysis assumes a single cohort.
weight	(Optional) A vector of case weights of the same length as success or an unquoted reference (name) to a column in data if it is specified. If success consists of counts instead of success indicators (1/0), then weight should also be specified to indicate the group size.

data	(Optional) A data frame containing the variables of interest. If data is specified, then success, group, and cohort will be searched within it.
di_80_index_cutoff	A numeric value between 0 and 1 that is used to determine disproportionate impact if the index comparing the success rate of the current group to the reference group falls below this threshold; defaults to 0.80.
reference_group	The reference group value in group that each group should be compared to in order to determine disproportionate impact. By default (= 'hpg'), the group with the highest success rate is used as reference. The user could also specify a value of 'overall' to use the overall rate as the reference for comparison, or 'all but current' to use the combined success rate of all other groups excluding the current group for each comparison.
check_valid_reference	Check whether reference_group is a valid value; defaults to TRUE. This argument exists to be used in di_iterate as when iterating DI calculations, there may be some scenarios where a specified reference group does not contain any students.

Details

This function determines disproportionate impact based on the 80% index method, as described in [this](#) reference from the California Community Colleges Chancellor's Office. It assumes that a higher rate is good ("success"). For rates that are deemed negative (eg, rate of drop-outs, high is bad), then consider looking at the converse of the non-success (eg, non drop-outs, high is good) instead in order to leverage this function properly.

Value

A data frame consisting of:

- cohort (if used),
- group,
- n (sample size),
- success (number of successes for the cohort-group),
- pct (proportion of successes for the cohort-group),
- reference_group (the reference group used to compare and determine disproportionate impact),
- reference (the reference rate used for comparison, corresponding to reference_group),
- di_80_index (ratio of pct to the reference),
- di_indicator (1 if di_80_index < di_80_index_cutoff),
- success_needed_not_di (the number of additional successes needed in order to no longer be considered disproportionately impacted as compared to the reference), and
- success_needed_full_parity (the number of additional successes needed in order to achieve full parity with the reference).

References

California Community Colleges Chancellor's Office (2014). [Guidelines for Measuring Disproportionate Impact in Equity Plans](#).

Examples

```
library(dplyr)
data(student_equity)
di_80_index(success=Transfer, group=Ethnicity, data=student_equity) %>%
  as.data.frame
```

di_iterate	<i>Iteratively calculate disproportionate impact using multiple method for many variables.</i>
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Description

Iteratively calculate disproportionate impact via the percentage point gap (PPG), proportionality index, and 80% index methods for many success variables, disaggregation variables, and scenarios.

Usage

```
di_iterate(
  data,
  success_vars,
  group_vars,
  cohort_vars = NULL,
  scenario_repeat_by_vars = NULL,
  exclude_scenario_df = NULL,
  weight_var = NULL,
  include_non_disagg_results = TRUE,
  ppg_reference_groups = "overall",
  min_moe = 0.03,
  use_prop_in_moe = FALSE,
  prop_sub_0 = 0.5,
  prop_sub_1 = 0.5,
  di_prop_index_cutoff = 0.8,
  di_80_index_cutoff = 0.8,
  di_80_index_reference_groups = "hpg",
  check_valid_reference = TRUE
)
```

Arguments

data	A data frame for which to iterate DI calculations for a set of variables.
success_vars	A character vector of success variable names to iterate across.
group_vars	A character vector of group (disaggregation) variable names to iterate across.

cohort_vars	(Optional) A character vector of the same length as success_vars to indicate the cohort variable to be used for each variable specified in success_vars. A vector of length 1 could be specified, in which case the same cohort variable is used for each success variable. If not specified, then a single cohort is assumed for all success variables.
scenario_repeat_by_vars	(Optional) A character vector of variables to repeat DI calculations for across all combination of these variables. For example, the following variables could be specified: <ul style="list-style-type: none"> • Ed Goal: Degree/Transfer, Short-term Career, Non-credit • First time college student: Yes, No • Full-time status: Yes, No Each combination of these variables (eg, full time, first time college students with an ed goal of degree/transfer as one combination) would constitute an iteration / sample for which to calculate disproportionate impact for outcomes listed in success_vars and for the disaggregation variables listed in group_vars. The overall rate of success for full time, first time college students with an ed goal of degree/transfer would just include these students and not others. Each variable specified is also collapsed to an '- All' group so that the combinations also reflect all students of a particular category. The total number of combinations for the previous example would be (+1 representing the all category): $(3 + 1) \times (2 + 1) \times (2 + 1) = 36$.
exclude_scenario_df	(Optional) A data frame with variables that match scenario_repeat_by_vars for specifying the combinations to exclude from DI calculations. Following the example specified above, one could choose to exclude part-time non-credit students from consideration.
weight_var	(Optional) A character variable specifying the weight variable if the input data set is summarized (ie, the the success variables specified in success_vars contain count of successes). Weight here corresponds to the denominator when calculating the success rate. Defaults to NULL for an input data set where each row describes each individual.
include_non_disagg_results	A logical variable specifying whether or not the non-disaggregated results should be returned; defaults to TRUE. When TRUE, a new variable '-None' is added to the data set with a single data value '-All', and this variable is added group_vars as a disaggregation/group variable. The user would want these results returned to review non-disaggregated results.
ppg_reference_groups	Either 'overall', 'hpg', 'all but current', or a character vector of the same length as group_vars that indicates the reference group value for each group variable in group_vars when determining disproportionate impact using the percentage point gap method.
min_moe	The minimum margin of error to be used in the PPG calculation, passed to di_ppg .
use_prop_in_moe	Whether the estimated proportions should be used in the margin of error calculation by the PPG, passed to di_ppg .

prop_sub_0	passed to di_ppg ; defaults to 0.50.
prop_sub_1	passed to di_ppg ; defaults to 0.50.
di_prop_index_cutoff	Threshold used for determining disproportionate impact using the proportionality index; passed to di_prop_index ; defaults to 0.80.
di_80_index_cutoff	Threshold used for determining disproportionate impact using the 80% index; passed to di_80_index ; defaults to 0.80.
di_80_index_reference_groups	A character vector of the same length as <code>group_vars</code> that indicates the reference group value for each group variable in <code>group_vars</code> when determining disproportionate impact using the 80% index; defaults to 'hpg' (highest performing group as reference), but could also be 'overall' or 'all but current'.
check_valid_reference	Check whether <code>ppg_reference_groups</code> and <code>di_80_index_reference_groups</code> contain valid values; defaults to TRUE.

Details

Iteratively calculate disproportionate impact via the percentage point gap (PPG), proportionality index, and 80% index methods for all combinations of `success_vars`, `group_vars`, and `cohort_vars`, for each combination of subgroups specified by `scenario_repeat_by_vars`.

Value

A summarized data set (data frame) consisting of:

- `success_variable` (elements of `success_vars`),
- `disaggregation` (elements of `group_vars`),
- `cohort` (values corresponding to the variables specified in `cohort_vars`,
- `di_indicator_ppg` (1 if there is disproportionate impact per the percentage point gap method, 0 otherwise),
- `di_indicator_prop_index` (1 if there is disproportionate impact per the proportionality index, 0 otherwise),
- `di_indicator_80_index` (1 if there is disproportionate impact per the 80% index, 0 otherwise), and
- other relevant fields returned from [di_ppg](#), [di_prop_index](#), and [di_80_index](#).

Examples

```
library(dplyr)
data(student_equity)
# Multiple group variables
di_iterate(data=student_equity, success_vars=c('Transfer')
, group_vars=c('Ethnicity', 'Gender'), cohort_vars=c('Cohort')
, ppg_reference_groups='overall')
```

di_ppg	<i>Calculate disproportionate impact per the percentage point gap (PPG) method.</i>
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Description

Calculate disproportionate impact per the percentage point gap (PPG) method.

Usage

```
di_ppg(
  success,
  group,
  cohort,
  weight,
  reference = c("overall", "hpg", "all but current", unique(group)),
  data,
  min_moe = 0.03,
  use_prop_in_moe = FALSE,
  prop_sub_0 = 0.5,
  prop_sub_1 = 0.5,
  check_valid_reference = TRUE
)
```

Arguments

success	A vector of success indicators (1/0 or TRUE/FALSE) or an unquoted reference (name) to a column in data if it is specified. It could also be a vector of counts, in which case weight (group size) should also be specified.
group	A vector of group names of the same length as success or an unquoted reference (name) to a column in data if it is specified.
cohort	(Optional) A vector of cohort names of the same length as success or an unquoted reference (name) to a column in data if it is specified. Disproportionate impact is calculated for every group within each cohort. When cohort is not specified, then the analysis assumes a single cohort.
weight	(Optional) A vector of case weights of the same length as success or an unquoted reference (name) to a column in data if it is specified. If success consists of counts instead of success indicators (1/0), then weight should also be specified to indicate the group size.
reference	Either 'overall' (default), 'hpg' (highest performing group), 'all but current' (success rate of everyone excluding the comparison group; also known as 'ppg minus 1'), a value from group (specifying a reference group), a single proportion (eg, 0.50), or a vector of proportions (one for each cohort). Reference is used as a point of comparison for disproportionate impact for each group. When cohort is specified:

- 'overall' will use the overall success rate of each cohort group as the reference;
- 'hpg' will use the highest performing group in each cohort as reference;
- 'all but current' will use the calculated success rate of each cohort group excluding the comparison group
- the success rate of the specified reference group from group in each cohort will be used;
- the specified proportion will be used for all cohorts;
- the specified vector of proportions will refer to the reference point for each cohort in alphabetical order (so the number of proportions should equal to the number of unique cohorts).

data	(Optional) A data frame containing the variables of interest. If data is specified, then success, group, and cohort will be searched within it.
min_moe	The minimum margin of error (MOE) to be used in the calculation of disproportionate impact and is passed to ppg_moe . Defaults to 0.03.
use_prop_in_moe	A logical value indicating whether or not the MOE formula should use the observed success rates (TRUE). Defaults to FALSE, which uses 0.50 as the proportion in the MOE formula. If TRUE, the success rates are passed to the proportion argument of ppg_moe .
prop_sub_0	For cases where proportion is 0, substitute with prop_sub_0 (defaults to 0.5) to account for the zero MOE. This is relevant only when use_prop_in_moe=TRUE.
prop_sub_1	For cases where proportion is 1, substitute with prop_sub_1 (defaults to 0.5) to account for the zero MOE. This is relevant only when use_prop_in_moe=TRUE.
check_valid_reference	Check whether reference is a valid value; defaults to TRUE. This argument exists to be used in di_iterate as when iterating DI calculations, there may be some scenarios where a specified reference group does not contain any students.

Details

This function determines disproportionate impact based on the percentage point gap (PPG) method, as described in [this](#) reference from the California Community Colleges Chancellor's Office. It assumes that a higher rate is good ("success"). For rates that are deemed negative (eg, rate of drop-outs, high is bad), then consider looking at the converse of the non-success (eg, non drop-outs, high is good) instead in order to leverage this function properly. Note that the margin of error (MOE) is calculated using $1.96 * \sqrt{0.25^2/n}$, with a `min_moe` used as the minimum by default.

Value

A data frame consisting of:

- cohort (if used),
- group,
- n (sample size),
- success (number of successes for the cohort-group),

- pct (proportion of successes for the cohort-group),
- reference_group (reference group used in DI calculation),
- reference (reference value used in DI calculation),
- moe (margin of error),
- pct_lo (lower 95% confidence limit for pct),
- pct_hi (upper 95% confidence limit for pct),
- di_indicator (1 if there is disproportionate impact, ie, when pct_hi <= reference),
- success_needed_not_di (the number of additional successes needed in order to no longer be considered disproportionately impacted as compared to the reference), and
- success_needed_full_parity (the number of additional successes needed in order to achieve full parity with the reference).

References

California Community Colleges Chancellor's Office (2017). [Percentage Point Gap Method](#).

Examples

```
library(dplyr)
data(student_equity)
# Vector
di_ppg(success=student_equity$Transfer
, group=student_equity$Ethnicity) %>% as.data.frame
# Tidy and column reference
di_ppg(success=Transfer, group=Ethnicity, data=student_equity) %>%
  as.data.frame
# Cohort
di_ppg(success=Transfer, group=Ethnicity, cohort=Cohort
, data=student_equity) %>%
  as.data.frame
# With custom reference (single)
di_ppg(success=Transfer, group=Ethnicity, reference=0.54
, data=student_equity) %>%
  as.data.frame
# With custom reference (multiple)
di_ppg(success=Transfer, group=Ethnicity, cohort=Cohort
, reference=c(0.5, 0.55), data=student_equity) %>%
  as.data.frame
# min_moe
di_ppg(success=Transfer, group=Ethnicity, data=student_equity
, min_moe=0.02) %>%
  as.data.frame
# use_prop_in_moe
di_ppg(success=Transfer, group=Ethnicity, data=student_equity
, min_moe=0.02
, use_prop_in_moe=TRUE) %>%
  as.data.frame
```

di_ppg_iterate	<i>Iteratively calculate disproportionate impact via the percentage point gap (PPG) method for many variables.</i>
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Description

Iteratively calculate disproportionate impact via the percentage point gap (PPG) method for many disaggregation variables.

Usage

```
di_ppg_iterate(
  data,
  success_vars,
  group_vars,
  cohort_vars,
  reference_groups,
  repeat_by_vars = NULL,
  weight_var = NULL,
  min_moe = 0.03,
  use_prop_in_moe = FALSE,
  prop_sub_0 = 0.5,
  prop_sub_1 = 0.5
)
```

Arguments

data	A data frame for which to iterate DI calculation for a set of variables.
success_vars	A character vector of success variable names to iterate across.
group_vars	A character vector of group (disaggregation) variable names to iterate across.
cohort_vars	A character vector of cohort variable names to iterate across.
reference_groups	Either 'overall', 'hpg', or a character vector of the same length as 'group_vars' that indicates the reference group value for each group variable in 'group_vars'.
repeat_by_vars	A character vector of variables to repeat DI calculations for across all combination of these variables, including '- All' as a group for each variable. The reference rate used for DI comparison differs for every combination of the variables listed here.
weight_var	A character scalar specifying the weight variable if the input data set is summarized (ie, the the success variables specified in 'success_vars' contain count of successes). Weight here corresponds to the denominator when calculating the success rate. Defaults to 'NULL' for an input data set where each row describes each individual.
min_moe	The minimum margin of error to be used in the PPG calculation, passed to 'di_ppg'.

use_prop_in_moe	Whether the estimated proportions should be used in the margin of error calculation by the PPG, passed to 'di_ppg'.
prop_sub_0	Passed to 'di_ppg'.
prop_sub_1	Passed to 'di_ppg'.

Details

Iteratively calculate disproportionate impact via the percentage point gap (PPG) method for all combinations of 'success_vars', 'group_vars', and 'cohort_vars', for each combination of subgroups specified by 'repeat_by_vars'.

Value

A data frame with all relevant returned fields from 'di_ppg' plus 'success_variable' (elements of 'success_vars'), 'disaggregation' (elements of 'group_vars'), and 'reference_group' (elements of 'reference_groups').

Examples

```
library(dplyr)
data(student_equity)
# Multiple group variables
di_ppg_iterate(data=student_equity, success_vars=c('Transfer')
, group_vars=c('Ethnicity', 'Gender'), cohort_vars=c('Cohort')
, reference_groups='overall')
```

di_prop_index	<i>Calculate disproportionate impact per the proportionality index (PI) method.</i>
---------------	---

Description

Calculate disproportionate impact per the proportionality index (PI) method.

Usage

```
di_prop_index(success, group, cohort, weight, data, di_prop_index_cutoff = 0.8)
```

Arguments

success	A vector of success indicators (1/0 or TRUE/FALSE) or an unquoted reference (name) to a column in data if it is specified. It could also be a vector of counts, in which case weight should also be specified (group size).
group	A vector of group names of the same length as success or an unquoted reference (name) to a column in data if it is specified.

cohort	(Optional) A vector of cohort names of the same length as <code>success</code> or an unquoted reference (name) to a column in data if it is specified. disproportionate impact is calculated for every group within each cohort. When <code>cohort</code> is not specified, then the analysis assumes a single cohort.
weight	(Optional) A vector of case weights of the same length as <code>success</code> or an unquoted reference (name) to a column in data if it is specified. If <code>success</code> consists of counts instead of success indicators (1/0), then <code>weight</code> should also be specified to indicate the group size.
data	(Optional) A data frame containing the variables of interest. If <code>data</code> is specified, then <code>success</code> , <code>group</code> , and <code>cohort</code> will be searched within it.
<code>di_prop_index_cutoff</code>	A numeric value between 0 and 1 that is used to determine disproportionate impact if the proportionality index falls below this threshold; defaults to 0.80.

Details

This function determines disproportionate impact based on the proportionality index (PI) method, as described in [this](#) reference from the California Community Colleges Chancellor's Office. It assumes that a higher rate is good ("success"). For rates that are deemed negative (eg, rate of drop-outs, high is bad), then consider looking at the converse of the non-success (eg, non drop-outs, high is good) instead in order to leverage this function properly.

Value

A data frame consisting of:

- `cohort` (if used),
- `group`,
- `n` (sample size),
- `success` (number of successes for the cohort-group),
- `pct_success` (proportion of successes attributed to the group within the cohort),
- `pct_group` (proportion of sample attributed to the group within the cohort),
- `di_prop_index` (ratio of `pct_success` to `pct_group`),
- `di_indicator` (1 if `di_prop_index` < `di_prop_index_cutoff`), and
- `success_needed_not_di` (the number of additional successes needed in order to no longer be considered disproportionately impacted as compared to the reference), and
- `success_needed_full_parity` (the number of additional successes needed in order to achieve full parity with the reference).

When `di_prop_index` < 1, then there are signs of disproportionate impact.

References

California Community Colleges Chancellor's Office (2014). [Guidelines for Measuring Disproportionate Impact in Equity Plans](#).

Examples

```
library(dplyr)
data(student_equity)
di_prop_index(success=Transfer, group=Ethnicity, data=student_equity) %>%
  as.data.frame
```

ppg_moe

*Margin of error for the PPG***Description**

Calculate the margin of error (MOE) for the percentage point gap (PPG) method.

Usage

```
ppg_moe(n, proportion, min_moe = 0.03, prop_sub_0 = 0.5, prop_sub_1 = 0.5)
```

Arguments

n	Sample size for the group of interest.
proportion	(Optional) The proportion of successes for the group of interest. If specified, then the proportion is used in the MOE formula. Otherwise, a default proportion of 0.50 is used (conservative and yields the maximum MOE).
min_moe	The minimum MOE returned even if the sample size is large. Defaults to 0.03. This equates to a minimum threshold gap for declaring disproportionate impact.
prop_sub_0	For cases where ‘proportion’ is 0, substitute with prop_sub_0 (defaults to 0.5) to account for the zero MOE.
prop_sub_1	For cases where ‘proportion’ is 1, substitute with prop_sub_1 (defaults to 0.5) to account for the zero MOE.

Value

The margin of error for the PPG given the specified sample size.

References

California Community Colleges Chancellor’s Office (2017). [Percentage Point Gap Method](#).

Examples

```
ppg_moe(n=800)
ppg_moe(n=c(200, 800, 1000, 2000))
ppg_moe(n=800, proportion=0.20)
ppg_moe(n=800, proportion=0.20, min_moe=0)
ppg_moe(n=c(200, 800, 1000, 2000), min_moe=0.01)
```

student_equity	<i>Fake data on student equity</i>
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Description

Data randomly generated to illustrate the use of the package.

Usage

```
data(student_equity)
```

Format

A data frame with 20,000 rows:

Ethnicity ethnicity (one of: Asian, Black, Hispanic, Multi-Ethnicity, Native American, White).

Gender gender (one of: Male, Female, Other).

Cohort year student first enrolled in any credit course at the institution (one of: 2017, 2018).

Transfer 1 or 0 indicating whether or not a student transferred within 2 years of first enrollment (Cohort).

Cohort_Math year student first enrolled in a math course at the institution; could be NA if the student have not attempted math.

Math 1 or 0 indicating whether or not a student completed transfer-level math within 1 year of their first math attempt (Cohort_Math); could be NA if the student have not attempted math.

Cohort_English year student first enrolled in a math course at the institution; could be NA if the student have not attempted math.

English 1 or 0 indicating whether or not a student completed transfer-level English within 1 year of their first math attempt (Cohort_English); could be NA if the student have not attempted English.

Ed_Goal student's educational goal (one of: Deg/Transfer, Other).

College_Status student's educational status (one of: First-time College, Other).

Student_ID student's unique identifier.

EthnicityFlag_Asian 1 (yes) or 0 (no) indicating whether or not a student self-identifies as Asian.

EthnicityFlag_Black 1 (yes) or 0 (no) indicating whether or not a student self-identifies as Black.

EthnicityFlag_Hispanic 1 (yes) or 0 (no) indicating whether or not a student self-identifies as Hispanic.

EthnicityFlag_NativeAmerican 1 (yes) or 0 (no) indicating whether or not a student self-identifies as Native American.

EthnicityFlag_PacificIslander 1 (yes) or 0 (no) indicating whether or not a student self-identifies as Pacific Islander.

EthnicityFlag_White 1 (yes) or 0 (no) indicating whether or not a student self-identifies as White.

EthnicityFlag_Caribbean 1 (yes) or 0 (no) indicating whether or not a student self-identifies as Caribbean.

EthnicityFlag_EastAsian 1 (yes) or 0 (no) indicating whether or not a student self-identifies as East Asian.

EthnicityFlag_SouthEastAsian 1 (yes) or 0 (no) indicating whether or not a student self-identifies as Southeast Asian.

EthnicityFlag_SouthWestAsianNorthAfrican 1 (yes) or 0 (no) indicating whether or not a student self-identifies as Southwest Asian / North African (SWANA).

EthnicityFlag_AANAPI 1 (yes) or 0 (no) indicating whether or not a student self-identifies as Asian-American or Native American Pacific Islander (AANAPI).

EthnicityFlag_Unknown 1 (yes) or 0 (no) indicating whether or not a student self-identifies as Unknown.

EthnicityFlag_TwoorMoreRaces 1 (yes) or 0 (no) indicating whether or not a student self-identifies as two or more races.

Examples

```
data(student_equity)
```

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